

11)



12) If $v = (a, b)$ then, since \mathbb{Z}_3 is a field, we can divide by a ($\neq a \neq 0$) to obtain

$$\hat{v} = (1, b/a)$$

But then if $p = x + sv$ then

$$p = x + (sa)\hat{v} \quad \text{as well,}$$

And vice-versa.

13) Four slopes: $0, 1, 2, \infty$.

14) Four lines thru origin, one for each slope,

15) Four points at ∞ , one for each slope

$$9 + 4 = 13 \text{ points total in } \mathbb{Z}_3 P^2,$$

16) Two additional lines parallel to each line in $(\mathbb{Z}_3)^2$,

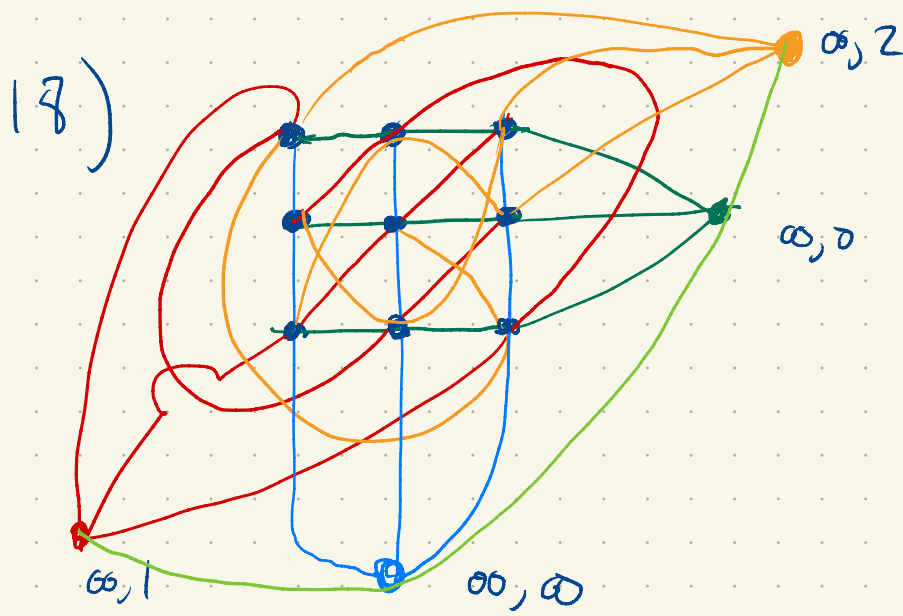
17) $3 \cdot (4) = 12$ lines in $\mathbb{Z}_3 P^2$

↑ ↑
parallel lines
copies thru
0

Add one line at infinity

for 13 lines in $\mathbb{Z}_3 P^2$.

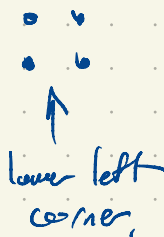
(13 points, 13 lines, duality!)



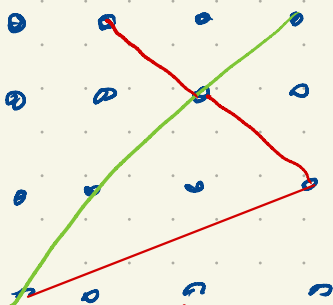
By stating, axioms 1, 2 are clear.

For four points, no three collinear, use

- $(0,0)$
- $(0,1)$
- $(1,0)$
- $(1,1)$



19)



Two lines that
intersect twice