$\Gamma(x) =$

In this worksheet we go through some guidelines (a recipe) for sketching the graph of a function using information that can be learned from calculus. In truth, in the modern era, computers and calculators are frequently used to graph functions. You should think of these exercises instead as pushups: nobody does pushups because they think that pushups are a good life skill. Rather, people do pushups to build upper-body strength to help them in other applications that they **do** think are useful. With that in mind, let's go through the steps for sketching our first curve.

You should also note that the guidelines presented here are just a little different from the ones presented in your text. Use either; I've presented mine here to emphasize what I think are helpful ways to approach this task and *think* about what you are doing.

- **1.** Sketch the graph of $f(x) = \frac{x}{1 + r^2}$.
 - **a**. Determine the domain of the function. You'll need to know this to decide on the set of *x*-values where you want to draw the sketch.

al red rumbers A marks : **b**. Decide if the function has any symmetry. Is it an even function (f(-x) = f(x))? An odd function (f(-x) = -f(x))? A periodic function? - χ) = $f(-\chi)$ = $f(-\chi)$ provide a bit of scaffolding for your sketch. Good candidates include x = 0 (i.e. computing the y-intercept) and finding roots (i.e. places where f(x) = 0). This step will vary function-by-function. (0) =

d. Determine if the function has any interesting behavior at $\pm \infty$. Is $\lim_{x\to\infty} f(x) = L$? Then there will be a horizontal asymptote at y = L. Or maybe $\lim_{x\to\infty} f(x) = \infty$ and the function blows up at infinity.



21 $\chi \rightarrow -\alpha$ 1-70 **e**. Determine if the function has any spots a where it blows up to $\pm \infty$ (i.e. $\lim_{x \to a} f(x) =$ $\pm\infty$). There will be vertical asymptotes at these locations. You can often spot these by division by zero or by know behavior of functions like $\ln(x)$.

No vertical asymptotes.

L = C

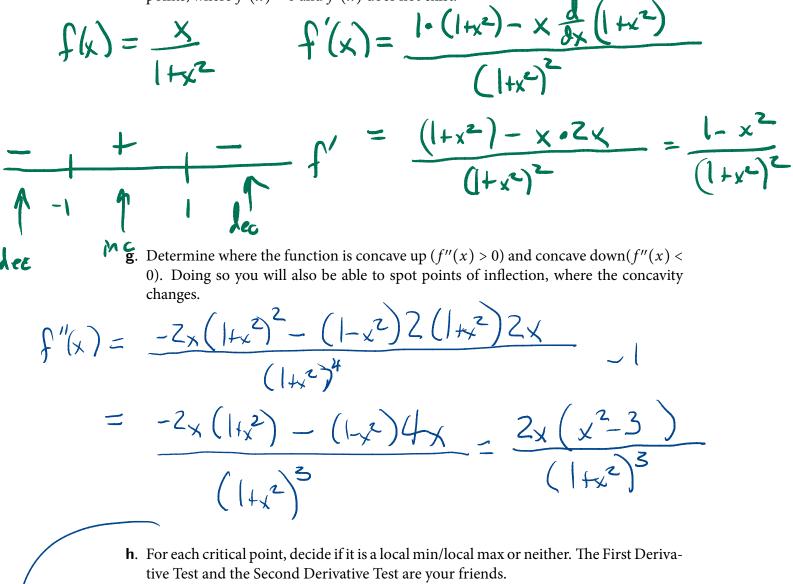
J3

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f"(1) < 0 => local max

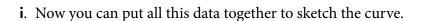
2"1(-1)70=7 local mil

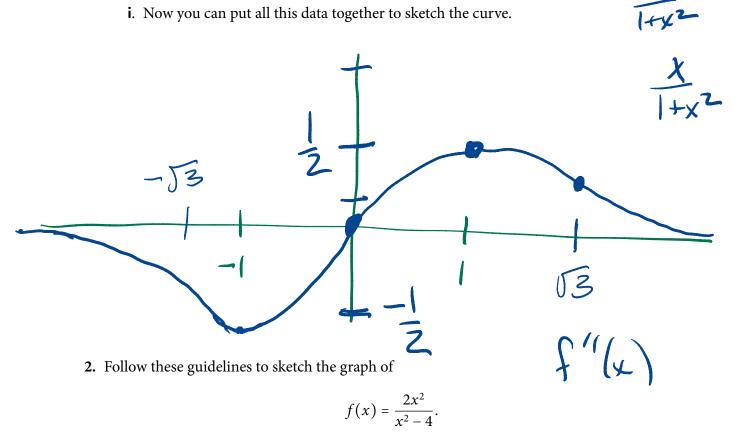
f. Determine where the function is increasing and where it is decreasing. I.e., decide where f'(x) > 0 and where f'(x) < 0. Doing so you will also determine critical points, where f'(x) = 0 and f'(x) does not exist.



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Critical points: X=1,-1





a. What is the function's domain?

b. Does this function have any symmetry?

c. Find a few choice values of x to evaluate the function at. In this case, what's the yintercept? Are there any roots?