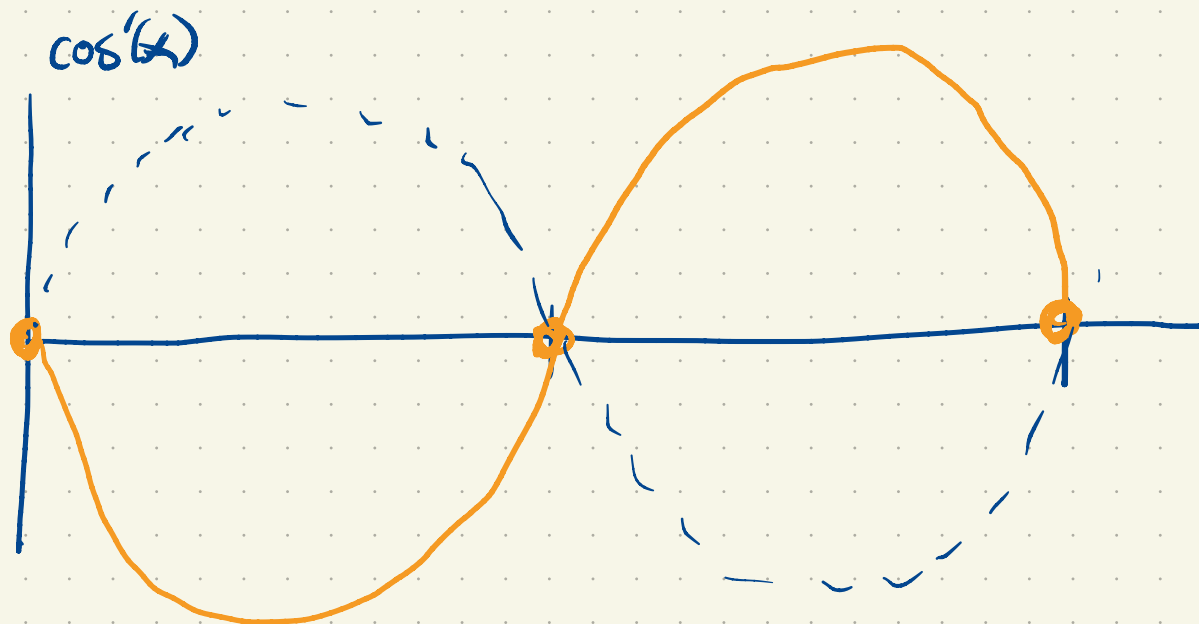
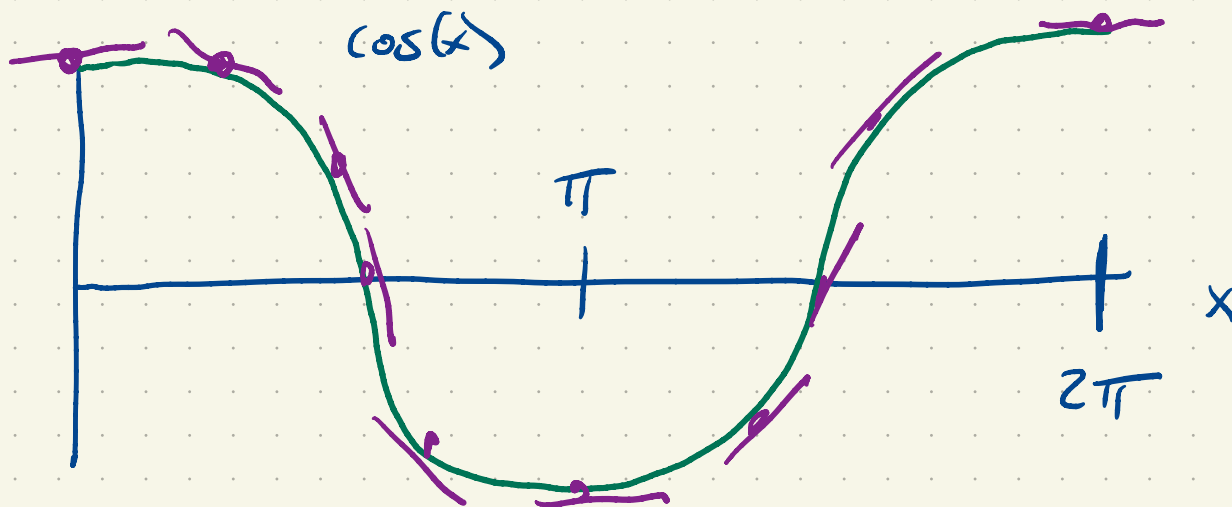
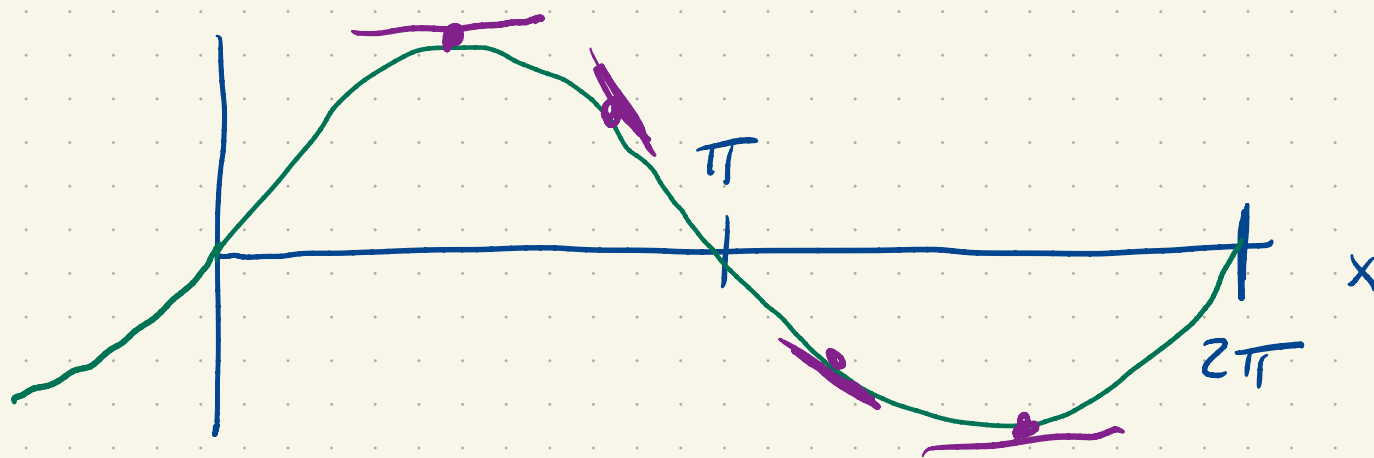


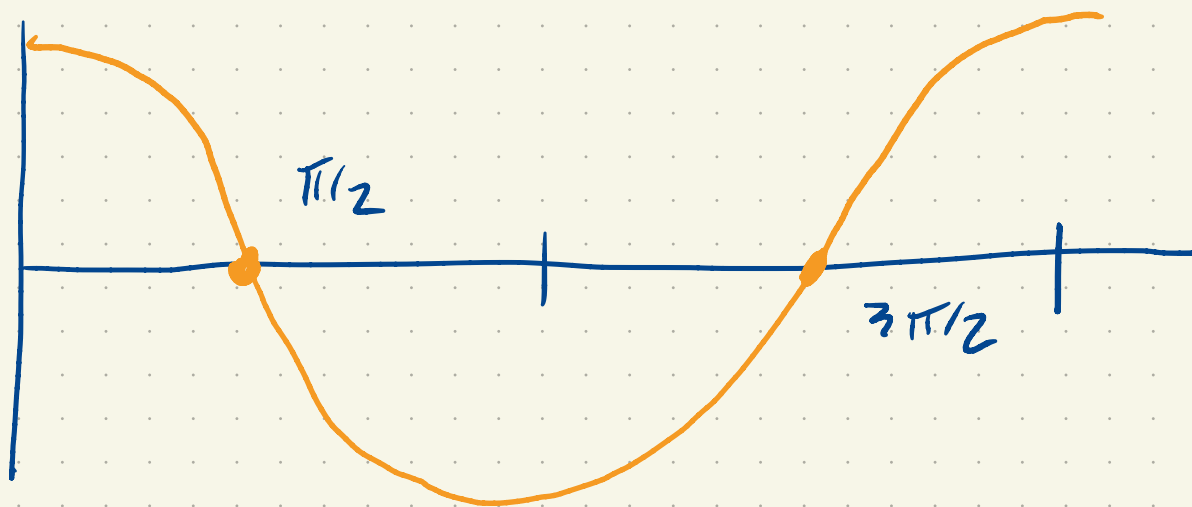
$$\frac{d}{dx} \cos(x) = -\sin(x)$$



$$\frac{d}{dx} \sin(x) = \cos(x)$$

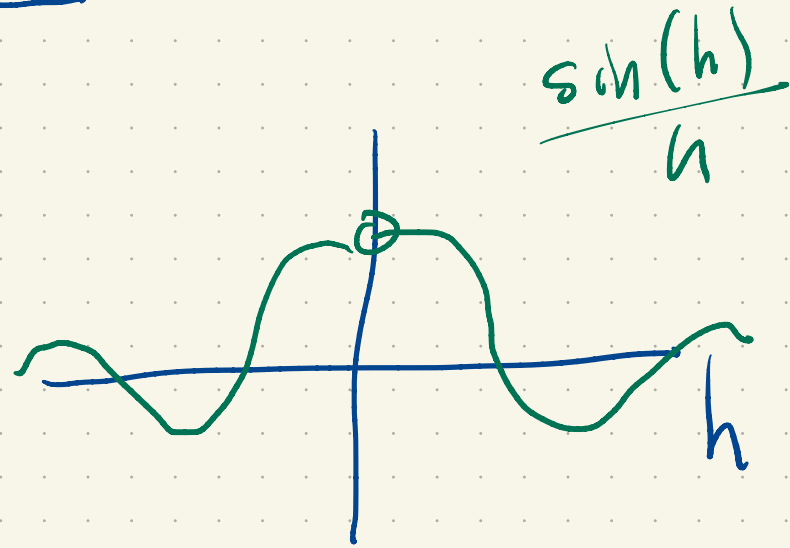


$\sin'(x)$



$$\sin'(0) = \lim_{h \rightarrow 0} \frac{\sin(0+h) - \sin(0)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\sin(h)}{h} = 1$$



$$\cos'(0) = \lim_{h \rightarrow 0} \frac{\cos(0+h) - \cos(0)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\cos(h) - 1}{h}$$

$$\sin'(0) = \lim_{h \rightarrow 0} \frac{\sin(0+h) - \sin(0)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\sin(h)}{h} = 1$$

- 0.05  
 - 0.005  
 - 0.0005

$$\cos'(0) = \lim_{h \rightarrow 0} \frac{\cos(0+h) - \cos(0)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\cos(h) - 1}{h}$$

$h$	$\frac{\cos(h) - 1}{h}$
0.1	-0.049...
0.01	-0.0049...
0.001	-0.00049...

$$\sin'(0) = \lim_{h \rightarrow 0} \frac{\sin(0+h) - \sin(0)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\sin(h)}{h} = 1$$

$$\cos'(0) = \lim_{h \rightarrow 0} \frac{\cos(0+h) - \cos(0)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\cos(h) - 1}{h} = 0$$

lovely

geometric  
proof

[see text!]

[see me!]

Last class:

$$\sec(x) = \frac{1}{\cos(x)}$$

$$\frac{d}{dx} \tan(x) = \frac{d}{dx} \frac{\sin(x)}{\cos(x)}$$

$$= \frac{\left[ \frac{d}{dx} \sin(x) \right] \cos(x) - \sin(x) \left[ \frac{d}{dx} \cos(x) \right]}{\cos^2(x)}$$

$$= \frac{\cos^2(x) + \sin^2(x)}{\cos^2(x)} = \frac{1}{\cos^2(x)}$$

Last class:

$$\frac{d}{dx} \tan(x) = \frac{d}{dx} \frac{\sin(x)}{\cos(x)}$$

$$= \frac{\left[ \frac{d}{dx} \sin(x) \right] \cos(x) - \sin(x) \left[ \frac{d}{dx} \cos(x) \right]}{\cos^2(x)}$$

$$= \frac{\cos^2(x) + \sin^2(x)}{\cos^2(x)} = \frac{1}{\cos^2(x)}$$

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$$\frac{d}{dx} \tan(x) = \sec^2(x)$$