

Important broccoli.

- $5^3 5^2 = (5 \cdot 5 \cdot 5)(5 \cdot 5) = 5^5$
- And  $r^a r^b = r^{a+b}$ .
- $(5^3)^2 = (5^3) \cdot (5^3) = 5^{2 \cdot 3}$
- And  $(r^a)^b = r^{ab}$
- $5^{-1} \cdot 5 = 5^0 = 1$  and therefore  $5^{-1} = 1/5$ .
- Also,  $r^{-1} = 1/r$
- $(2 \cdot 7)^2 = (2 \cdot 7)(2 \cdot 7) = 2^2 7^2$ .
- Also  $(rs)^a = r^a s^a$

Exponential functions (applied!)

- Exponential functions  $f(x) = a^x$  describe **doubling** or **halving** phenomena.
- They are different from power functions like  $p(x) = x^7$
- A population that doubles every year has the form  $g(t) = C 2^t$  for some constant  $C$ .
- A population that doubles every three years has the form  $g(t) = C 2^{t/3}$ .
- A population that halves every year has the form  $g(t) = C 2^{-t}$ .
- An account that grows at 10% every year has the form  $A(t) = C (1.1)^t$ .
- Sneak preview: you can write  $(1.1)^t$  as  $2^{at}$  for a particular number  $a$ . So this is also a doubling phenomenon.