

1. Starting from the formula  $e^{z_1} e^{z_2} = e^{z_1+z_2}$  for all complex numbers  $z_1$  and  $z_2$ , and using the fact that  $e^{i\theta} = \cos \theta + i \sin \theta$  for all  $\theta \in \mathbb{R}$ , show

$$\begin{aligned}\sin(\theta + \phi) &= \sin(\theta) \cos(\phi) + \cos(\theta) \sin(\phi) \\ \cos(\theta + \phi) &= \cos(\theta) \cos(\phi) - \sin(\theta) \sin(\phi).\end{aligned}$$

2. Use the results of problem 1) to show that  $SO(2)$  is a matrix group.
3. Text: 1.1.2
4. Text: 1.1.3
5. Derive the formulas  $R_{\theta_1} R_{\theta_2} = R_{\theta_1+\theta_2}$  and  $z_{\theta_1} z_{\theta_2} = z_{\theta_1+\theta_2}$ .
6. Text: 1.2.3 (You'll want to read page 6 first)
7. Text: 1.2.4
8. Text: 1.2.5