1. Find two numbers whose difference is 100 and whose product is a minimum.
2. Find the point on the line $6 x+y=9$ that is closest to the origin. Hint: minimizing distance is equivalent to minimizing distance squared!
3. A stadium curve is the curve that bounds a rectangular region with half circles at opposite ends of the rectangle; think of a running track. Find the dimensions of a stadium curve that maximize the area of the enclosed rectangle if the perimeter of the stadium curve is 440 yards.
4. A hiker is on the tundra two miles south of a road. The road runs east-west the hiker wishes to reach a point on the road 5 miles to the east. The hiker can travel at 3 mph on the tundra and 4 mph on the road. What path should the hiker take to minimize their travel time to their destination?
5. The USPS will accept a box for shipment if the sum of its length plus girth (total distance around) does not exceed 108 inches. What shape of box with a square end has maximum enclosed volume and is acceptable for shipping? You may assume that girth is measured as perimeter of the square.
6. An isosceles triangle has base 6 cm and height 12 cm . Find the maximum possible area of a rectangle that can be placed inside the triangle with one side on the base of the triangle.
