

The trunk of a tree is growing. The radius  $r$  of the trunk, in centimeters, is given by

$$r(t) = 2\sqrt{t}$$

where  $t$  is measured in years.

1. Find the average rate of change from  $t = 1$  to  $t = 2$  years.
2. Use the  $h$ -version of the limit definition of the derivative to find the instantaneous rate of change at  $t = 1$  year.

3. Use the  $a, b$ -version of the limit definition of the derivative to find the instantaneous rate of change of radius at  $t = 1$  year.

4. I promise you that  $r(4) = 4\text{cm}$  and  $r'(4) = 1/2 \text{ cm/year}$ . From this data alone, approximate the radius at 4 years and one month. Then compare your approximation with the true value.