Optimization:

We can use calculus in some settings to find "The best" option among many possibilities. Ofter best is formulated as biggest.

Suppose f is a function with domain R, suy. If c is a point in IR and if

- f(c) > f(x) for all x = R we
- say f(c) is an absolute muximum value of f.

 $f(x) = 1 - x^2$ on (-1, 1)e.g.

f(0) = is a markamum value for f(+)

If f(x)= 5 for all x, does f have a max value?

Where is the mass achieved?

We have a similar concept for minon um 5.

f(c) is an absolute minum where f(c) < f(c) < f(c) for all XER

Note: f from the previous example does not have an absolute maximum.

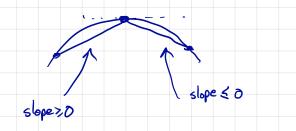
Functions need not have any absolute maxames or maintainess.

eg f(x)=ex

And they can have muliple:

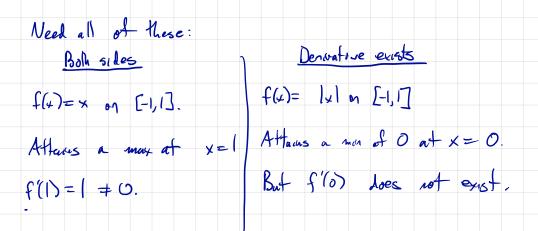
f(x) = 5.4(x) $f = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2}$ l is a may value - (is a min value

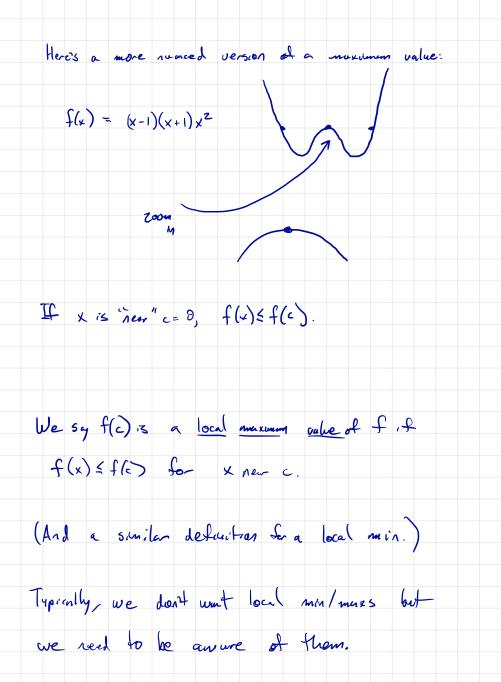
What does calculus have to do with this?



intuitarely slope of targent line there is 0.

Fact: If the homem of f contains an interval avoid c, ad of fattains a max or min atc, and of files exists, then files = 0.





Fact: If the lower of f contains an interval around c, ad of f attains a max on min atc, ad of f'(c) exists, Then f'(c) = 0. local This gives you a way to look for maxuna: Spots where f'(x) = 0
spots x where f is not defined on both sudes of x. It's gotta be one of these, I any where. 5 Def: we say a is a critical point for f A f'()=0 or f'() DNE.

 $f(x) = xe^{x}$ -1 -e' e.g. clearly doesn't have an

absolute max.

Could have an absolute man. $f'(x) = e^{x} + xe^{x} = (1+x)e^{x}$

f(x) = 0 at x = -1.

Indeed f(-D=-e' is a maximum value for f.

Now we have seen that functions need not have more (maxes.

Bat: If f is continuous on Ea, 6], a closel, bounded atend, then facturicues both a minimum and a maxiluum. (Extreme Value Theorem)