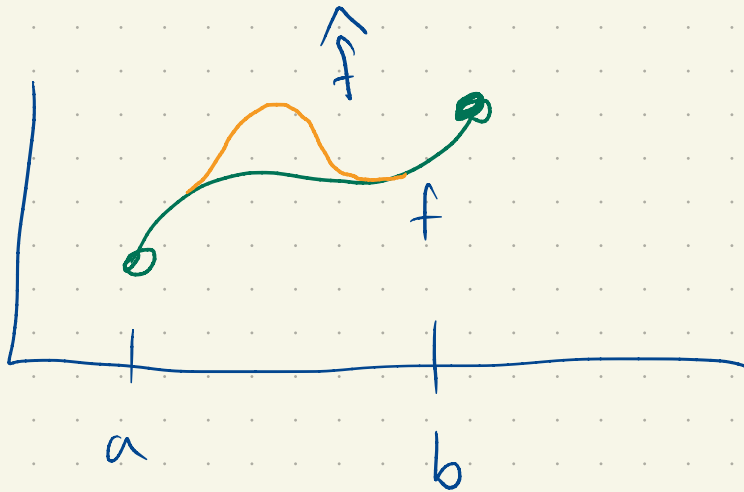


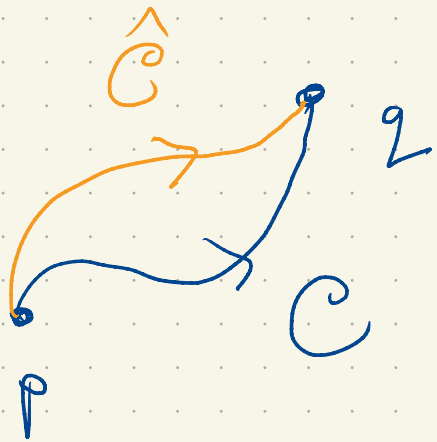
$$\oiint \vec{\nabla}_x \vec{Z} \cdot \vec{n} dS = \int_C \vec{Z} \cdot d\vec{r}$$



$$\int_a^b f'(x) dx = f(b) - f(a)$$

$$\int_a^b \hat{f}'(x) dx = \hat{f}(b) - \hat{f}(a)$$

$$= f(b) - f(a)$$

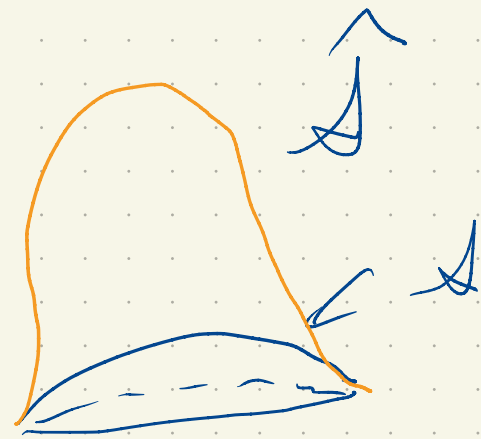


$$\int_C \vec{\nabla} f \cdot d\vec{r} = f(z) - f(p)$$

FTLI

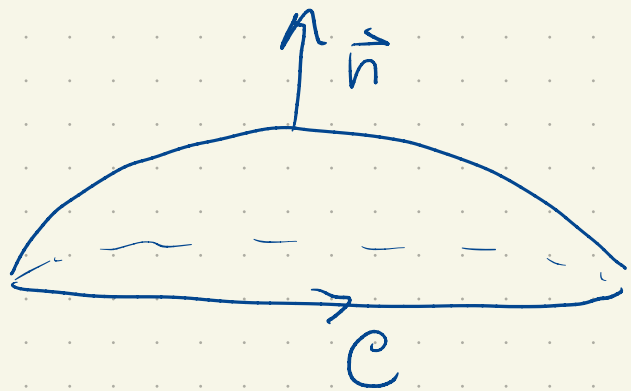
$$\int_C \vec{\nabla} f \cdot d\vec{r} \quad \text{vs} \quad \int_{\hat{C}} \vec{\nabla} f \cdot d\vec{r}$$

=



$$\iint_S (\vec{\nabla} \times \vec{z}) \cdot \vec{n} \, dS = \int_C \vec{z} \cdot d\vec{r}$$

$$\iint_S (\vec{\nabla} \times \vec{z}) \cdot \vec{n} \, dS \quad \text{vs} \quad \iint_S (\vec{\nabla} \times \vec{z}) \cdot \vec{n} \, dS$$



$$z = \sqrt{3}$$

$$x^2 + y^2 + z^2 = 4$$

$$z \geq \sqrt{3}$$

$$x^2 + y^2 \leq 1$$

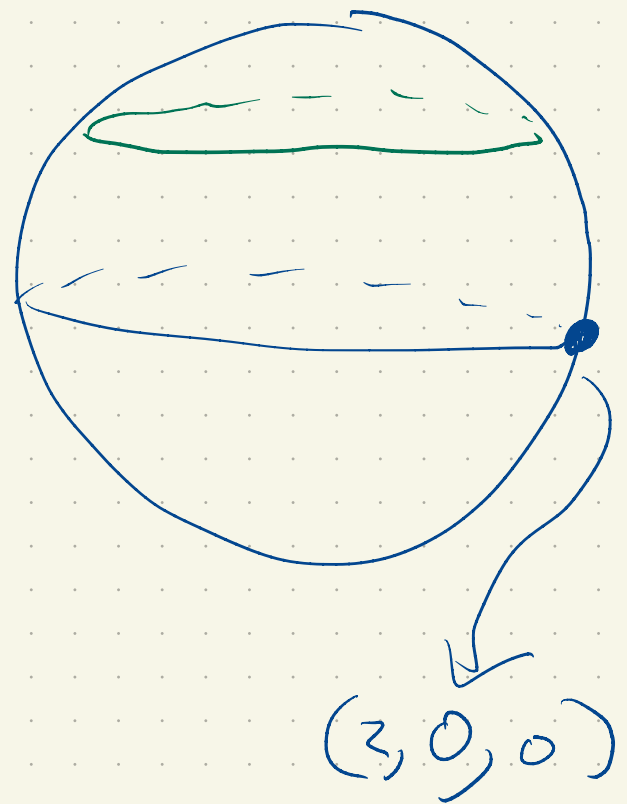
$$z = \pm \sqrt{4 - x^2 - y^2}$$

$$\vec{F} = \langle xz, yz+x, xy \rangle$$

$$\iint_{\Sigma} (\nabla \times \vec{F}) \cdot \vec{n} \, dS = \int_C \vec{F} \cdot d\vec{r}$$

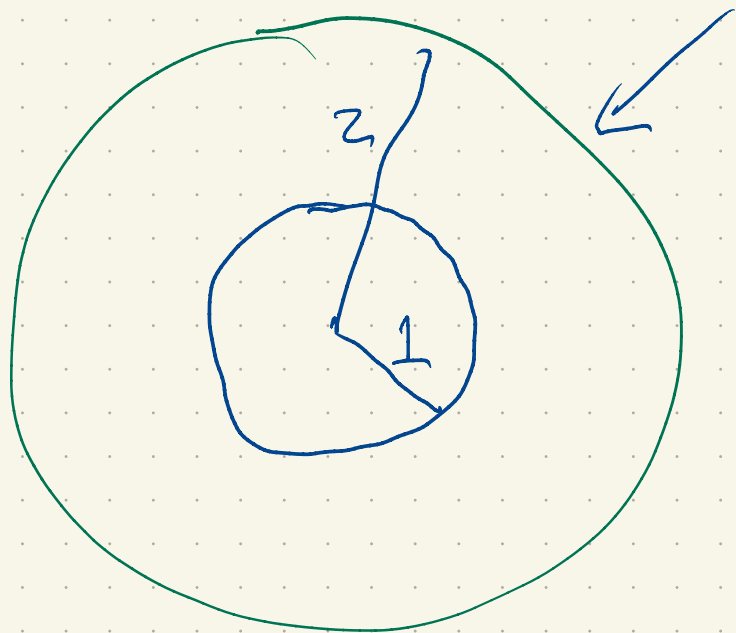
$\Sigma \quad \parallel \quad C$   
 $\pi \quad \quad \quad \pi$

$$\vec{r}(u, v) = \langle u, v, \sqrt{4 - u^2 - v^2} \rangle$$



$$(3, 0, 0)$$

$$u^2 + v^2 \leq 1$$



$$\vec{r}_u \times \vec{r}_v = \left\langle \frac{u}{\sqrt{4-u^2-v^2}}, \frac{v}{\sqrt{4-u^2-v^2}}, 1 \right\rangle$$

↑ points perp. to surface

$$\vec{\nabla}_x \vec{F} = \langle x-y, x-y, 1 \rangle$$

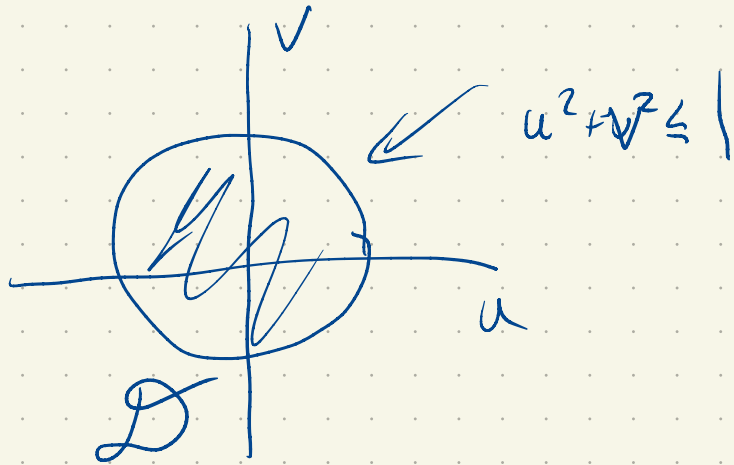
$$(\vec{\nabla}_x \vec{F})(\vec{r}(u,v)) = \langle u-v, u-v, 1 \rangle$$

$$\iint_{\mathcal{D}} (\vec{\nabla}_x \vec{F}) \cdot \vec{n} \, dS = \iint_{\mathcal{D}} (\vec{\nabla}_x \vec{F})(\vec{r}(u,v)) \cdot (\vec{r}_u \times \vec{r}_v) \, du \, dv$$

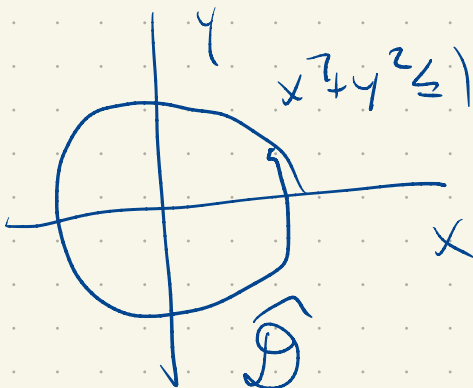
↑ region of  $u$ 's  $v$ 's that describes  $\mathcal{D}$

$$u^2 + v^2 \leq 1$$

$$= \pi$$

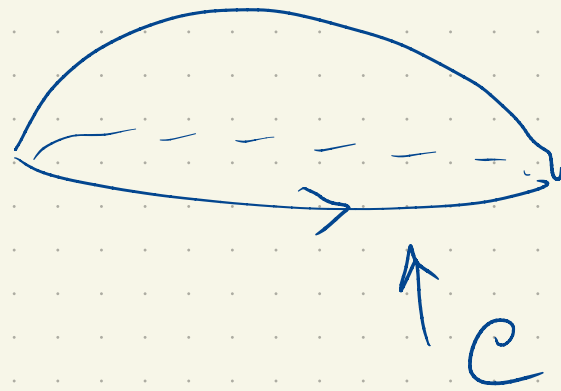


$$\iint_{\mathcal{D}} u^2 dA(u,v)$$



$$\iint_{\mathcal{D}} x dA(x,y)$$

$$\int_C \vec{F} \cdot d\vec{r}$$



$$x^2 + y^2 = 1$$
$$z = \sqrt{3}$$

$$\vec{\sigma}(t) = \langle \cos(t), \sin(t), \sqrt{3} \rangle$$

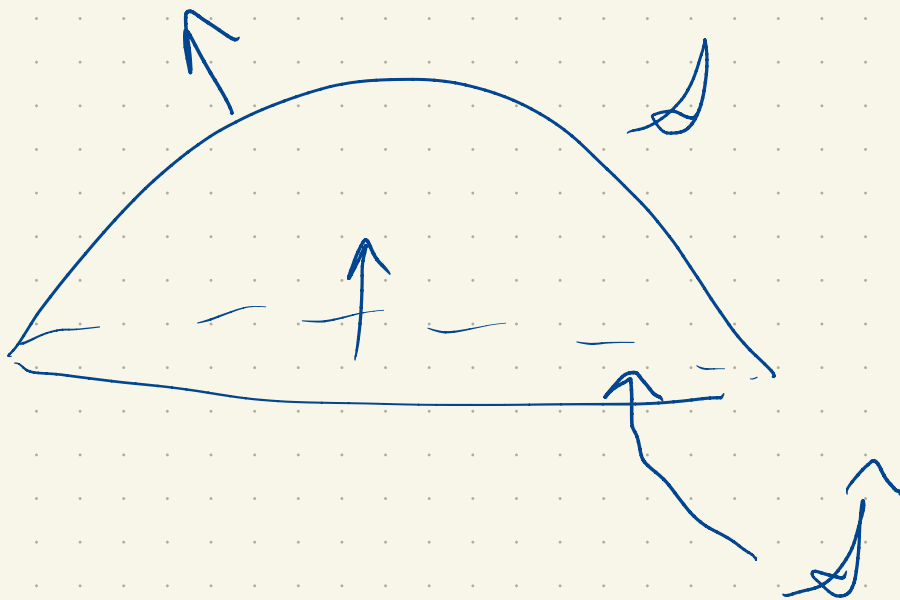
$$0 \leq t \leq 2\pi$$

$$\vec{F} = \langle xz, yz+x, xy \rangle$$

$$\vec{F}(\vec{\sigma}(t)) = \langle \sqrt{3}\cos(t), \sqrt{3}\sin(t) + \cos(t), \cos(t)\sin(t) \rangle$$

$$\vec{\sigma}'(t) = \langle -\sin(t), \cos(t), 0 \rangle$$

$$\int_C \vec{F} \cdot d\vec{s} = \int_0^{2\pi} \vec{F}(\vec{\sigma}(t)) \cdot \vec{\sigma}'(t) dt = \pi$$



$$\iint_S (\vec{\nabla}_x \vec{F}) \cdot \vec{n} \, dS = \pi$$

$$\iint_S (\vec{\nabla}_x \vec{F}) \cdot \vec{n} \, dS = \pi$$

$$\vec{r}(u, v) = \langle u, v, \sqrt{3} \rangle$$

$$\vec{\nabla}_x \vec{F} = \langle x-y, x-y, 1 \rangle$$

$$\vec{r}_u = \langle 1, 0, 0 \rangle$$

$$\vec{\nabla}_x \vec{F}(\vec{r}(u, v)) = \langle u-v, u-v, 1 \rangle$$

$$\vec{r}_v = \langle 0, 1, 0 \rangle$$

$$\vec{\nabla}_x \vec{F}(\vec{r}(u, v)) \cdot (\vec{r}_u \times \vec{r}_v) = 1$$

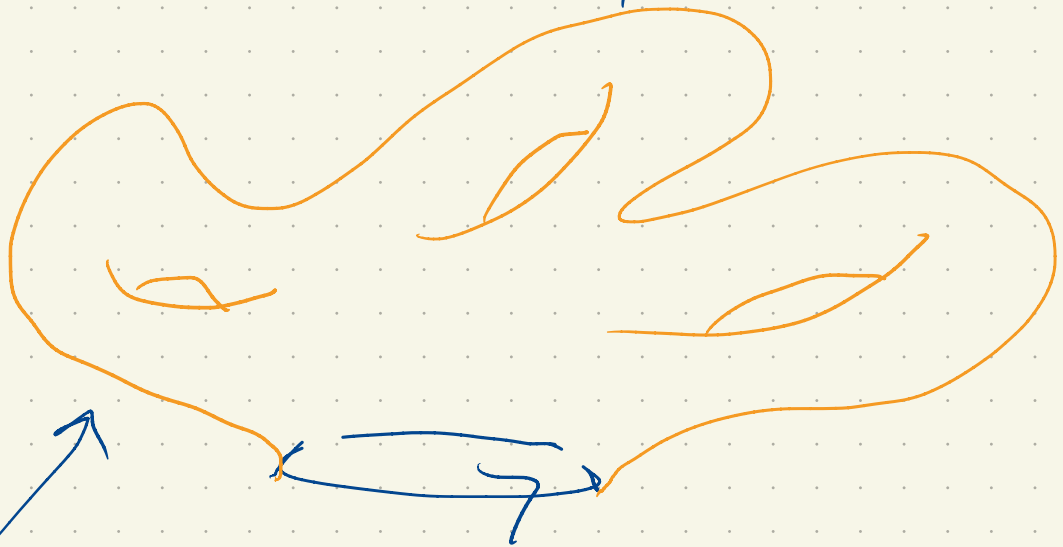
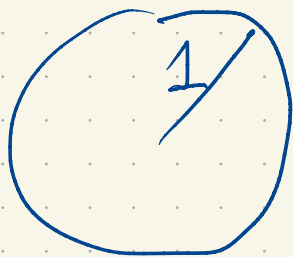
$$\vec{r}_u \times \vec{r}_v = \langle 0, 0, 1 \rangle$$

$$u^2 + v^2 \leq 1$$

$$\iint_{\mathcal{D}} (\vec{\nabla}_x \vec{F}) \cdot \vec{n} \, dS = \iiint_{\mathcal{D}} 1 \, du \, dv = \pi$$

$\mathcal{D}$

$$u^2 + v^2 \leq 1$$



$$\iint_{\mathcal{D}} (\vec{\nabla}_x \vec{F}) \cdot \vec{n} \, dS = \pi$$



$$\int_C \vec{F} \cdot d\vec{r} =$$